Abstract—In the second of two companion articles, a 54-year time series for the oyster population in the New Jersey waters of Delaware Bay is analyzed to examine how the presence of multiple stable states affects reference-point–based management. Multiple stable states are described by four types of reference points. Type I is the carrying capacity for the stable state; each has associated with it a type-II reference point wherein surplus production reaches a local maximum. Type-II reference points are separated by an intermediate surplus production low (type III). Two stable states establish a type-IV reference point, a point-of-no-return that impedes recovery to the higher stable state. The type-II to type-III differential in surplus production is a measure of the difficulty of rebuilding the population and the sensitivity of the population to collapse at high abundance. Surplus production projections show that the abundances defining the four types of reference points are relatively stable over a wide range of uncertainties in recruitment and mortality rates. The surplus production values associated with type-II and type-III reference points are much more uncertain. Thus, biomass goals are more easily established than fishing mortality rates for oyster populations.

Multiple stable reference points in oyster populations: implications for reference point-based management

Eric N. Powell (contact author)¹
John M. Klinck²
Kathryn A. Ashton-Alcox¹
John N. Kraeuter¹

Email address for contact author: eric@hsrl.rutgers.edu

¹ Haskin Shellfish Research Laboratory
Rutgers University
6959 Miller Ave.
Port Norris, New Jersey 08349
² Center for Coastal Physical Oceanography
Crittenton Hall
Old Dominion University
Norfolk, Virginia 23529

All federal fisheries, and some state fisheries, are managed under biological reference-point guidelines under which a specific yearly allocation or quota is advised to constrain fishing mortality (e.g., Wallace et al.¹). The biological reference-point approach for federal fisheries mandated by the Magnuson-Stevens Fishery Conservation and Management Act (Anonymous, 1996) requires management of fish populations at a biomass that provides maximum sustainable yield. In this system, sophisticated survey, analytical, and modeling procedures are used to identify selected biological reference points, such as the target biomass, $B_{msy}$, and the carrying capacity, $K$. Fishing mortality is then set in relation to reference point goals. Normally, $B_{msy}$ is defined in relation to carrying capacity; the biomass present without fishing, where natural mortality balances recruitment (e.g., May et al., 1978; Johnson, 1994; Mangel and Tier, 1994; Rice, 2001). This stable point is characterized by a population for which most animals are adults, where natural mortality rates are low, and where recruitment is limited by compensatory processes such as resource limitation constraining fecundity. $B_{msy}$ is most commonly defined as $\frac{K}{\alpha}$, based on the well-known Schaefer model that stipulates the guiding premise that surplus production is highest at $\frac{K}{\alpha}$ (Hilborn and Walters [1992]; see Restrepo et al. [1998] for more details on the federal management system).

The raison d'être for reference-point–based management is the development of equilibria between recruitment (and growth) and mortality at target host densities (the archetype being $B_{msy}$). Unfortunately, for managing oyster populations, obstacles exist in meeting this objective because oyster populations do not appear to be inherently equilibrivous, particularly those subjected to MSX, a disease caused by the protozoan Haplosporidium nelsoni, or Dermo, a disease caused by the protozoan Perkinsus marinus. Time series of oyster abundance typically show wide interannual variations, mediated in no small measure by year-to-year differences in natural mortality rate, although overfishing has also been an important contributing agent (e.g., Mann et al., 1991; Rothschild et al., 1994; Burreson and Ragone Calvo, 1996; Ragone Calvo et al., 2001; Jordan et al.¹)

al., 2002; Powell et al., 2008). In the first of two companion contributions, we described the case for oyster populations in Delaware Bay. A 54-year time series documents two regime shifts, circa-1970 and circa-1985, with intervening and succeeding intervals having the attributes of alternate stable states (sensu Gray, 1977; Peterson, 1984; Knowlton, 2004). Within these periods are substantial population excursions produced by varying rates of recruitment and natural mortality, but the alternate stable states are demarcated by even larger excursions in abundance. Moreover, these periods of relative stability delineated by regime shifts are persistent and transcend a range of climatic conditions (Soniat et al., in press).

Population dynamics of the Delaware Bay oyster population is not solely a function of disease, but stable-point abundances are at least partially a byproduct of disease, and disease has played a role in regime shifts (Powell et al., 2008). The classic view of carrying capacity fails when disease accounts for a substantial fraction of natural mortality and this compromises an estimate of $B_{msy}$. Some have attempted to redefine carrying capacity in diseased populations in relation to the abundance (population density in classic disease models, e.g., Kermack and McKendrick (1991), Hethcote and van den Driessche (1995)] at which each diseased animal will produce, in its lifetime, a single infection event (e.g., Heesterbeek and Roberts, 1995; Swinton and Anderson, 1995). This abundance is always below, usually well below, the original $K$. When abundance rises above this level, the influence of disease increases, as does the chance of epizootic mortality. This increase restrains population abundance below the predisease $K$ (e.g., Kermack and McKendrick, 1991; Hasibeder et al., 1992; Godfray and Briggs, 1995; Frank, 1996). This approach is not well tailored to diseases such as MSX and Dermo for which environment is a potent moderator of effect and in which rapid transmission rates are not requiring of host-to-host contact. Furthermore, the existence of multiple apparently stable states and regime shifts imply that the standard Schaefer model, from which such basic biological references points as $B_{msy}$ are derived, also does not provide the appropriate framework for managing oyster populations because this model has only a single stable state.

These ratiocinations lead to three salient questions pertinent to developing management goals for oyster stocks: 1) Can reference points be defined that consistently permit fishing without jeopardizing the sustainability of the stock? 2) Must management goals be set within the context of each of several multiple stable states? 3) How does regime change affect the usefulness of reference points and can management goals be set to increase the probability of regime shift to a preferred stable state? In this contribution, we use the case of the Delaware Bay oyster stock in New Jersey waters to examine these questions. In a companion contribution, we describe the long-term survey time series and the relationships of broodstock abundance with recruitment and mortality (Powell et al., 2009). In this contribution, we develop a surplus production model to relate these relationships with stock performance over a range of abundances. Following discussion of the results of simulations with this model, we consider the basis for an MSY-based management system for oyster populations and the implications of multiple stable states in the decision-making process.

Model formulations and statistics

Powell et al. (2008, 2009) have provided an overview of the oyster populations in Delaware Bay during the 1953–2006 time period. Analyses of the Delaware Bay oyster resource of New Jersey routinely reveal a division between the upbay group of eight beds (Round Island, Upper Arnolds, Arnolds, Upper Middle, Middle, Sea Breeze, Cohanssey, and Ship John) and the downbay group of twelve beds (Shell Rock, Bennies Sand, Bennies, New Beds, Hog Shoal, Hawk’s Nest, Strawberry, Vexton, Beadons, Egg Island, Nantuxent Point, Sand, Bennies). Salinity, natural mortality rate, and growth rate are higher downbay. Dredge efficiencies are significantly higher downbay (Powell et al., 2002, 2007). Both regions can be subdivided on the basis of natural mortality rate and productivity. In the upbay group, natural mortality rates and growth rates are significantly lower for the upper three beds, Round Island, Upper Arnolds and Arnolds, than for the remaining beds. Henceforth these two groups will be termed the low-mortality and medium-mortality beds (Table 1). In the downbay group, growth rates and mortality rates are lower for Shell Rock, leading to its designation as a medium-mortality bed; the reminder are high-mortality beds (Table 1).

<table>
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<tr>
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<td>High mortality</td>
<td>Bennies Sand, Bennies, New Beds, Hog Shoal, Hawk’s Nest, Strawberry, Vexton, Beadons, Egg Island, Nantuxent Point, Sand, Bennies</td>
</tr>
</tbody>
</table>

Table 1

The bed groups (by location: upbay and downbay) and subgroups (by mortality rate) for the eastern oyster (Crassostrea virginica) collected on twenty beds in Delaware Bay, as shown in Figure 1. Mortality rate divides each of the primary groups, themselves being divided by location, a surrogate for upbay-downbay variations in dredge efficiency and fishery-area management regulations.
The twenty natural oyster beds of the eastern oyster (*Crassostrea virginica*) in the New Jersey waters of Delaware Bay may be characterized in terms of high-quality (dark shade) and medium-quality (light shade) grids. The term “quality” refers to a relative differential in long-term average oyster abundance (Powell et al., 2008). The footprints for the Middle bed (upper portion of figure) and the beds downbay from it, except New Beds, Egg Island, and Ledge, were updated with data from surveys in 2005 and 2006. The footprints for the remaining beds were based on historical definitions.

Throughout this contribution, we will refer to these bay regions where necessary, but in general, we will model the entire stock. In the following section, we summarize the biological relationships identified by Powell et al. (2009) without further discussion.

Natural mortality fractions were obtained from box counts (*bc*) under the assumption that

\[ N_{\text{oysters}_{t-1}} = N_{\text{boxets}} + N_{\text{liveoysters}} , \]

where \( N \) = the number of individuals.

Hence,

\[ \Phi_{bc} = \frac{N_{\text{boxets}}}{N_{\text{boxets}} + N_{\text{liveoysters}}} , \]

where \( \Phi_{bc} \) = the fraction of the individuals alive at the end of year \( t \) that died during the next year.
The fraction dead determined from box counts is related to the natural mortality rate \( m_{bc} \) as

\[
m_{bc} = - \frac{\log_e (1 - \Phi_{bc})}{t},
\]

where \( t \) = time.

Boxes do not adequately measure the mortality of juvenile animals. The fraction dying not recorded by box counts, \( \Phi_0 \), is obtained by difference:

\[
\Phi_0 = \frac{(N_t - N_{t-1}) - (R_{t-1} - \Phi_{bc} N_{t-1} - \Phi_f N_{t-1})}{N_{t-1} + R_{t-1}},
\]

where \( \Phi_f \) is the fraction taken by the fishery; 
\( R \) = the number of recruits into the population; and the first parenthetical term on the right-hand side represents the difference in abundance between two consecutive surveys.

The two natural mortality rates, \( m_{bc} \) (Eq. 3) and \( m_0 \) (Eq. 5), are additive (sensu Hassell et al., 1982; Holmes, 1982), as the method for estimation includes the box counts as an input (Eq. 2) in contrast to fishing mortality that can be compensatory under certain fishing season scenarios (Klinck et al., 2001). \( \Phi_0 \) varied randomly over the time series with a 54-year mean of 0.274 and a 54-year median of 0.311 (Powell et al., 2008). The mortality rate can be obtained from \( \Phi_0 \) as

\[
m_0 = - \frac{\log_e (1 - \Phi_0)}{t}.
\]

Fishing mortality was calculated as the fraction of the population present at the beginning of the year removed during that year by the fishery (catch):

\[
\Phi_f = \frac{\text{catch}}{N_{t-1}}.
\]

Additional mortality associated with the dredging process may occur; however, Powell et al. (2001, 2004) determined that this source of mortality was inconsequential in comparison to the catch. Since the late 1950s, the fishery has rarely removed more than 7% of the stock annually, and normally much less, so that the yearly changes in stock abundance in Delaware Bay have been dominantly a product of natural processes over much of the time series (Powell et al., 2008).

A crude estimate of age-frequency pattern was obtained by assuming equilibrium conditions. Yearlings, \( Y \), were estimated from recruits (spat), \( R \), based on observed one-year survivals of recruits between 1953 and 1988 when yearlings were recorded as part of the survey. The yearling-to-spat ratio followed a weakly nonrandom pattern (Fig. 2) that provides a relationship between recruits and yearlings described by

\[
Y_{t+1} = 0.434e^{-3.659\times10^{-11}N_t R_t},
\]

Older age groups were modeled by assuming equivalent mortality across all ages. Thus, the number at age \( a \) is estimated as

\[
N_a = Y e^{-\alpha (m_0 + m_{bc})},
\]

where \( m_0 \) and \( m_{bc} \) are from Equations 5 and 3, respectively.

To model the relationship between broodstock abundance and recruitment, we fit a relationship that produces declining recruitment at high abundance (overcompensation sensu Hancock, 1973; McCann et al., 2003), because shellfish can achieve densities sufficient to limit growth and reproduction (e.g., Fréchette and Bourget, 1985; Fréchette and Lefaivre, 1990; Powell et al., 1995). Thus, from Hilborn and Walters (1992)

\[
\tilde{R} = \tilde{N}_{t-1} e^{-\frac{N_{t-1}}{\beta}},
\]

where \( \tilde{R} \) = the number of spat in millions; and \( \tilde{N}_{t-1} \) = oyster abundance in millions.
The recruitment rate \( \Gamma_t(\tilde{N}_{t-1}) \) is calculated as

\[
\log_e \left( 1 + e^{-\left(1 + \frac{\tilde{N}_{t-1}}{\beta} \right)} \right) = \frac{\Gamma_t(\tilde{N}_{t-1})}{t}.
\]

(10)

We compared the results of Equation 10 to that obtained for a best-fit linear regression with zero intercept. The linear relationship is

\[ R_t = 0.493 N_{t-1}. \]

(11)

Note that the linear fit travels through the recruitment values at low abundance slightly below that traversed by the Ricker curve (Fig. 8 in Powell et al., 2009). Powell et al. (2009) provide caveats concerning the use of a single broodstock–recruitment curve for the population over the entire 54-yr time series. The dispersion of the stock over the four bay regions exerts limitations on the ambit of stock performance at any specific time.

Powell et al. (2009) develop an admittedly ad hoc empirical relationship to describe the relationship between box-count mortality and abundance:

\[
\Phi_{bc} = \omega + \chi \log_e \left( \tilde{N}_{t-1} + \rho \right) - \frac{\left( \frac{\tilde{N}_{t-1}}{\nu^2} \right)}{2
\]

(12)

where \( \omega=0.055, \chi=0.03, \rho=1.0, \psi=0.0025, \chi=0.1, \psi=2.2, \) and \( \nu=0.8, \) with \( N \) expressed as billions of animals.

The specific mortality rate, \( m_{bc}(N) \), is calculated with Equation 3. Equation 12 has the unique property of eliciting both depressant and compensatory trends at low abundance. Powell et al. (2009) provide caveats concerning the use of the broodstock–mortality curve. The dispersion of the stock over the four bay regions exerts limitations on the ambit of stock performance at any specific time. At abundances greater than \( 4 \times 10^9 \), mortality was low. The fraction dying each year averaged 9.6 % for these nonepizooic years, a nonepizooic year being defined for convenience as a year in which the fraction dying is less than 20%. However, of the 32 years with abundances less than \( 3 \times 10^9 \), of which 14 were epizooic years, only one had a fractional mortality between 0.15 and 0.20. Accordingly, two divergent outcomes exist over a range of low abundances. In some years, the fraction dying approximates the long-term mean for high-abundance years, about 9.6%. In other years, epizooic mortalities occur. The likelihood of these two divergent outcomes is substantively affected by the dispersion of the stock (Powell et al., 2009).

Surplus production \( S \) is calculated as the difference between additions to the population through recruitment and debits through mortality. The two processes are structurally uncoupled in time, however. First, mortality occurs differentially in time in relation to recruitment. Second, the method of data collection results in a time-integrated value of mortality, but a year ending value for recruitment, inasmuch as the death of recruits between settlement and the time of observation is not recognized as a component of the mortality term (see Keough and Downes, 1982; Powell et al., 1984; Caffey, 1985). Consequently, in the absence of fishing,

\[
S_t = N_{t-1} \left( e^{\Gamma t} - 1 \right) - N_{t-1} \left( 1 - e^{-m_{bc} \rho^\Gamma t} \right),
\]

(13)

which reduces to the familiar equation

\[
S_t = N_{t-1} e^{-m_{bc} \rho^\Gamma t} + R_t,
\]

(14)

where \( t \) is the time increment between observations of recruitment.

Note that the subscript \( t-1 \) is used for the stock abundance value \( N \) because the stock survey occurs at the end of the year preceding the year for which surplus production is forecast and for which recruitment is measured.

Modeling of population dynamics—results of simulations and discussion

In the absence of fishing, the population increases when surplus production \( S_t \) is positive (Eq. 14). The population decreases when \( S_t \) is negative. Abundances where \( S_t \) is zero offer potential biological reference points, as do cases where \( S_t \) is maximal. Carrying capacity is an example of the former. In this case, mortality and recruitment balance and \( S_t=0 \). Surplus production declines as abundance nears carrying capacity and, therefore, the rate of change should be negative, but relatively constant; thus, \( \frac{dS}{dN} < 0 \) and \( \frac{dS}{dN} \approx 0 \). We will refer to reference points characterized by \( S_t=0 \), \( \frac{dS}{dN} < 0 \) and \( \frac{dS}{dN} \approx 0 \) as type-I reference points (Fig. 3). \( B_{masy} \) is defined to be a maximum in surplus production. Surplus production declines as abundance declines below or rises above this point. Hence, \( S_t > 0 \), \( \frac{dS}{dN} = 0 \) and \( \frac{dS}{dN} < 0 \). We will refer to maxima in surplus production as type-II reference points (Fig. 3). Because the time series under analysis is configured in terms of abundance rather than biomass, the designation \( N_{masy} \) rather than \( B_{masy} \) will be used hereafter.

We present hereafter a series of simulations of the Delaware Bay oyster stock designed to examine the change in surplus production with abundance. We first consider a population for which recruitment rate follows Equation 9, a compensatory curve, with a 54-yr average unrecorded mortality rate (Eq. 5), and with the box-count mortality rate described by Equation 12.
These relationships are depicted in Figures 7 and 10 of Powell et al. (2009). The trajectory for surplus production under these constraints is compared in Figure 3 and detailed in Figure 4. Recruitment rate rises as abundance declines (Fig. 4). This is anticipated from the compensation inherent in the relationship between broodstock and recruitment. The box-count mortality rate shows a maximum somewhat above an abundance of $2 \times 10^6$ (Fig. 4). These relationships define a trend between surplus production and abundance that is divergent from the normal Schaefer curve (Ricker, 1975; Hilborn and Walters, 1992; Haddon, 2001; Zabel, 2003), as expected. The single type-I reference point is at $N = 9.3 \times 10^9$. This is an estimate of carrying capacity, $K$. Typically a single type-II reference point would exist, $N_{msy}$, at about $\frac{K}{2}$, but in this case two maxima in surplus production exist, one higher, $N^H_{msy}$, than the other, $N^L_{msy}$. $N^H_{msy}$ is at $N = 4.86 \times 10^9$. This is the abundance classically interpreted as $N_{msy}$ and, indeed, surplus production is maximal at this point and the value is approximately $\frac{K}{2}$. The second type-II reference point occurs at $N = 1.43 \times 10^9$. Unlike the simple Schaefer curve depicted in Hilborn and Walters (1992), Haddon (2001), and Zabel (2003), a local minimum in surplus production exists between these two type-II surplus production maxima, at $N = 2.57 \times 10^9$. In this case, surplus production remains above zero, $S_r > 0$. An increase in abundance above this level and a decrease in abundance below this level both increase surplus production. This reference point, herein designated type III, always occurs between two maxima in surplus production and is characterized by $\frac{dN}{dS} = 0$ and $\frac{d^2N}{dS^2} > 0$ (Table 2). The unusual nature of the surplus production curve in Figure 4, that yields the local minimum in surplus production and a secondary surplus production peak at a lower abundance, is produced by the compensatory and compensatory segments of the box-count mortality relationship established by the relationship between the occurrence of epizootics and abundance in the Delaware Bay oyster stock.

Figures 5–7 show three alternative trajectories for the change in surplus production with abundance in the Delaware Bay oyster stock obtained by small modifications of the parameters governing recruitment and mortality. The first is obtained by using the 54-yr median unrecorded mortality rate, rather than the 54-yr mean rate. The median is distinctly higher. Again, the surplus production trajectory includes one type-I, two type-II, and one type-III reference points (Figs. 3 and 5). The abundance associated with the four reference points remains unchanged, although the surplus production values associated with the type-II maxima and type-III minimum are lower than in the preceding case (Table 2).

The second alternative is obtained after a perusal of Figure 10 in Powell et al. (2009) that shows that the mortality rate for stock abundances frequented by epizootics often falls below the curve provided by Equation 12. This is a function of stock dispersion that modulates the likelihood of epizootic mortality rates (Powell et al., 2009). In fact, on the average, box-count mortality rate reaches epizootic levels only half the time. Thus, Figures 3 and 6 show the trend in surplus production when epizootics are assumed to occur only half the time, and box-count mortality rate is expressed as the average of a year with an epizootic and a year without one. The type-III reference point is nearer the $N^L_{msy}$ value in this surplus production trajectory, so that the valley between $N^L_{msy}$ and $N^R_{msy}$ is something more than a shoulder on the surplus production curve. Thus, the value of the surplus production maxima, averaged over a number of years, is strongly influenced by the frequency and intensity of epizootics (Table 2).

The final alternative addresses the uncertainty that exists in the shape of the broodstock–recruitment curve at low abundance. Linearizing the curve at low abundance (Eq. 11) yields a surplus production trajectory depicted in Figure 8 of Powell et al. (2009). The relationship is unique in generating a second type-I reference point.

![Figure 3](image-url)

**Figure 3**

The trajectories of surplus production for cases detailed in Figures 4–7, with the locations of the four types of reference point indicated. Note that a type-IV reference point and two type-I reference points exist in only one case, Figure 7.
point, at \( N = 1.93 \times 10^9 \). This is a multiple-stable-point system with two carrying capacities, one at \( K_H \) and one at \( K_L \). Note that the lower surplus production maximum is closer to \( K_L \) than expected by the Schaefer relationship: \( N_{\text{msy}}^L > \frac{K}{2} \) (Fig. 7). This representation of oyster population dynamics also generates a type-IV reference point at \( N = 3.03 \times 10^9 \). Type IV, like type I, is characterized by \( S = 0 \) and \( \frac{dS}{dN} > 0 \), but in this case \( \frac{dN}{dS} > 0 \) (Table 2). Figure 8 presents a stylized version of the surplus production trajectory of Figure 7. Note that the type-I reference points are points of convergence. Abundance rising above this value will produce negative surplus production and a return to the abundance level and vice versa for a decline in abundance. On the other hand, type-IV reference points are divergences or points of persistence. A population reaching a type-IV reference point as abundance declines will see a rapid further decline. Once below this point, the likelihood becomes very low that the population can cross the gulf and re-acquire its high-abundance trajectory.

Reference-point–based management

**Carrying capacity** Perusal of the time series suggests that population abundances above about \( 12 \times 10^9 \) are unstable. The analyses provided using Equation 14 return this same expectation, that carrying capacity is about \( 9.3 \times 10^9 \). This explains the stability of population abundance during the 1970s as the population was at or near carrying capacity (Fig. 9). Abundance rose above this point a number of times between 1970 and 1985, but higher abundances were not sustainable. Interestingly, this carrying capacity is a carrying capacity for a population enzootic for MSX disease. The natural mortality rate during the 1970s is not much different from the few measures that exist for the time frame pre-1957 and the pre-MSX years are not outliers on the broodstock-recruitment curve, average unrecorded (mostly juvenile) mortality, and a box-count mortality rate that emphasizes epizootic mortality at low abundance. Catch estimates are conditional on the assumption of long-term persistence of a chosen abundance level and distribution of the entire stock in habitats permitting growth to market size.

![Figure 4](image.png)

**Figure 4**

The relationship of surplus production (Eq. 14), the rates of recruitment, unrecorded mortality, box-count mortality, and a conditional estimate of catch expressed as the fraction of the stock, for parameters defined by, for recruitment, \( \Gamma \), from Equation 10, \( m_y \) from Equation 5 using the 54-year average \( \Phi_b \) and \( m_y \) from Equation 12. This simulation assumes compensation in the broodstock–recruitment curve, average unrecorded (mostly juvenile) mortality, and a box-count mortality rate that emphasizes epizootic mortality at low abundance. Catch estimates are conditional on the assumption of long-term persistence of a chosen abundance level and distribution of the entire stock in habitats permitting growth to market size.

<table>
<thead>
<tr>
<th>Type I</th>
<th>II</th>
<th>Type I</th>
<th>Type II</th>
<th>Type IV</th>
<th>( S )</th>
<th>( \frac{dS}{dN} )</th>
<th>( \frac{d^2S}{dN^2} )</th>
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<tr>
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<td>( N_{\text{msy}}^L )</td>
<td>( \Phi_b )</td>
<td>( m_y )</td>
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</tbody>
</table>

**Table 2**

The surplus production values associated with the types I, II, III, and where applicable, IV reference points depicted in the referenced figures and the defining characteristics of each reference point type. Surplus production is expressed in billions of oysters. NA=not applicable.
Differential in abundance in the 1950s primarily a result of the higher fishing mortality rates during that time. Carrying capacity is defined by a set of criteria that are normally thought to be unique (Table 2). Interestingly, in Delaware Bay oyster populations, a second type-I reference point may exist, depending on the presence of a reference point of type IV, as considered subsequently. This type-I reference point, if present, is at $1.93 \times 10^9$, nearly a factor of 5 lower in abundance than the classic carrying capacity. However, this value is also similar to the abundance observed during the low-abundance phase of the population (Fig. 9), an outcome anticipated of a population with multiple stable points (Gray, 1977; Peterson, 1984) in which community compositions are theorized to resolve themselves into preferred states that can be exchanged only through triggering mechanisms capable of overcoming the inertia of the individual states. Soniat et al. (1998) argued that inertia is an important attribute of oyster populations capable of overcoming the inertia minimizes the influence of short-term environmental shifts. The 54-year time series of Delaware Bay supports the importance of inertia and suggests some reasons for how population dynamics are internally stabilized.

Both recruitment and mortality have abundance-dependent rates. The high-abundance regime is inherently stable. Mean first passage times (sensu Rothschild and Mullen, 1985; Redner, 2001; Rothschild et al., 2005) for transitions to the alternate stable state typically exceed 6 yr (Powell et al., 2009). Given a population at high abundance: that population will tend to maintain itself because high abundance, on the average, generates higher recruitment, and also, on the average, is associated with lower rates of natural mortality. Thus, high abundances have a strong internal self-sustaining mechanism. However, the 1970–85 period occurred prior to the onset of Dermo disease in Delaware Bay. Whether a high abundance state is sustainable under any environmental conditions with Dermo as the principal agent of mortality is unknown.

The low-abundance regime is stable only if the surplus production minimum separating the two maxima is negative. The differential between the two carrying capacities, $K^H$ and $K^L$, is a factor of 4.82. Powell et al. (2009) discuss the tendency for the Delaware Bay oyster population to contract to a habitat of refuge on the medium-mortality beds (Table 1) as abundance falls. This occurs due to the gradient in natural mortality that increasingly penalizes the population downestuary. The differential in bed area between the entire bay and the medium-mortality beds is a factor of 2.46 excluding the two lowermost and least productive beds, Egg Island and Ledge, or 2.70 including them. Thus, habitat area, though likely a contributor to the differential in the two carrying capacities, does not explain adequately the differential between $K^L$ and $K^H$, and this agrees with the observation (Figure 5 in Powell et al., 2009) that contracted and dispersed population distributions both prevailed for extended periods during the low-abundance regime.

**Surplus production targets** Beverton et al. (1984) distinguish between short-term catch forecasts used to generate a yearly TAL and long-term strategic assessments used to set abundance goals. The constant-abundance reference point implemented with the model of Klinck et al. (2001) is particularly useful in maintaining a population close to an abundance target and has been used for short-term catch forecasts but does not lend itself to long-term strategic assessments. The purpose of this study was to develop reference points that might be used to set abundance goals.

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**Figure 5**

The relationship of surplus production (Eq. 14), the rates of recruitment, unrecorded mortality, and box-count mortality, and a conditional estimate of catch expressed as the fraction of the stock, for parameters defined by, for recruitment, $\Gamma_l$ from Equation 10, $m_0$ from Equation 5 using the 54-year median $\phi_{I_{54}}$ and $m_{I_{54}}$ from Equation 12. This simulation assumes compensation in the broodstock-recruitment curve, median unrecorded (mostly juvenile) mortality, and a box-count mortality rate that emphasizes epizootic mortality at low abundance. This simulation differs from the simulation in Figure 4 in a higher level of unrecorded mortality. Catch estimates are conditional on the assumption of long-term persistence of a chosen abundance level and distribution of the entire stock in habitats permitting growth to market size.
Four types of reference points are elucidated. Each of them marks critical spots in the ambit of oyster population dynamics that must be included in a successful management plan. If the oyster population in Delaware Bay has two distinct regimes, minimally, two sets of reference points exist. It is a critical corollary of the multiple-stable-state theorem that such should be the case. Modern fisheries management scientists, although cognizant of the importance of regime shifts, have not yet inculcated the concept of multiple stable states into management philosophy and, consequently, continue to focus solely on the highest abundance state.

Maximum sustainable yield generally is considered to occur at half carrying capacity. For the high-abundance regime, \( N^L_{msy} \) occurs at almost precisely \( \frac{N}{2} \) (Figs. 3–7), as expected from standard fisheries theory (Haddon, 2001; Zabel et al., 2003). For the low-abundance regime, \( N^H_{msy} \) occurs at a value distinctly above \( \frac{N}{2} \); thus the lower surplus production dome is distinctly skewed. Some portion of this skewness may be inadequate extrapolation of the population dynamics to abundances below \( 0.8 \times 10^9 \) that have not yet been observed. Either \( N^H_{msy} \) or \( N^L_{msy} \) might be chosen as abundance goals. \( N^H_{msy} \) yields the highest surplus production and, consequently, the highest fishery yield, and, all else being equal, would be the desirable goal for rebuilding oyster abundance above present-day levels. Over the 54-year time series for Delaware Bay, the abundance level has been near carrying capacity for about one-third of the years and well below \( N^H_{msy} \) for most of the remaining years (Fig. 9). Thus, historical observations provide credence for the viability of this abundance goal.

However, an alternative exists, \( N^L_{msy} \). This second type-II reference point exists at lower abundance and maximizes fishery yield in the low-abundance regime (Fig. 9). The population has been near this level for about two-thirds of the years since 1953 and, for most of this time, this population dynamic has been little influenced by fishing mortality. Thus, a substantive choice exists in managing the Delaware Bay oyster stock. Is it a viable choice to seek through management to transition the population to the high-abundance state and thereby rebuild the population to the higher \( N^H_{msy} \) target?

The relationship of surplus production (Eq. 14), the rates of recruitment, unrecorded mortality, and box-count mortality, and a conditional estimate of catch expressed as the fraction of the stock, for parameters defined by, for recruitment, \( \Gamma \) from Equation 10, \( m_o \) from Equation 5 using the 54-year median \( \phi_o \), and \( m_{uc} \) from Equation 12. This simulation assumes compensation in the broodstock–recruitment curve, median unrecorded (mostly juvenile) mortality, but a box-count mortality rate that de-emphasizes epizootic mortality at low abundance. Epizootics are assumed to occur in half of the years when abundance is in the correct range, in comparison to the simulations shown in Figures 4 and 5. Surplus production as plotted is the average of an epizootic and a nonepizootic year. Catch estimates are conditional on the assumption of long-term persistence of a chosen abundance level and distribution of the entire stock in habitats permitting growth to market size.

The impact of type-III and type-IV reference points

The two other reference points become important at this juncture. The type-III reference point describes the valley between the two surplus production maxima. If negative, two stable states exist, associated with the lower and higher maxima in surplus production (e.g., Fig. 7). If positive, one stable state exists. The other lower maximum in surplus production is a quasi-stable state (e.g., Figs. 4–6). Surrounding the surplus production minimum is a region in which unwise harvest goals could create a region of negative surplus production and establish through overharvesting the second and lower stable state. Thus, this reference point is a measure of the relative degree of impedance present in the population dynamics to transiting to the higher stable state. This impedance exists naturally and is a rebuilding obstacle for management. This impedance can be deepened by inappropriate harvest goals.

If the minimum in surplus production is below zero, the type-IV reference point above it marks the thresh-
old for population collapse or the point-of-no-return abundance (e.g., Collie et al., 2004) below which the population is unlikely to regain the higher abundance state (Fig. 8). It is the critical point generating the regime shift from high abundance to low abundance. That is, once abundance drops to this point, abundance will resolutely fall to the lower carrying capacity and the population subsequently will resist the reverse course even in the absence of fishing (Fig. 8). Once crossed, no anthropogenic manipulation short of Herculean measures to enhance abundance will allow the population to recover. In the years succeeding the 1985 MSX epizootic, population abundance increased to levels representative of the type-III and type-IV reference points a number of times, falling back below these barriers in one to two years (Fig. 9). Two occurrences are noteworthy, one during 1987–89 before the onset of Dermo and one during 1996–98 after Dermo replaced MSX as the dominant disease agent causing mortality. In both cases, the population failed to successfully cross the type-IV barrier. In neither case was fishing responsible for this failure.

Uncertainty in the natural mortality rate presents a critical impediment to successful stock assessment (e.g., Beverton et al., 1984; Clark, 1999; Bradbury and Tagart, 2000). The population trajectories shown in Figures 3–7 differ principally in the degree and type of uncertainty in mortality and that controls the amplitude of the surplus production excursion between the lower type-II and upper type-II points, as well as the existence of a type-IV reference point. The rarity of regime shifts in the observed time series, the observed stability of the stable states, and the long mean first passage times for some population shifts (Powell et al., 2009) all suggest that the valley between regimes is difficult to cross. Thus, very likely the surplus production minimum in the Delaware Bay oyster stock is below zero or nearly so (Fig. 9). The population “resists” the flip between stable states and the degree of this “resistance” is a function of the depth and breadth of the valley between surplus production maxima.

The existence of the type-IV reference point influences management in two ways. If the population is above it, adequate precaution must be included to limit the probability of a population decline of this magnitude as close to zero as possible. The precautionary approach is a standard component in management (e.g., FAO, 1995; Restrepo et al., 1998), but the assessment of risk is rarely undertaken (e.g., Francis and Shotton, 1997). Note in Figure 7 that the type-IV point is closer to \( N^H_{\text{msy}} \) than \( N^H_{\text{msy}} \) is to \( K^H \). Thus, management at \( MSY \) carries with it an increased risk of stock collapse. On the other hand, if the population is below the type-IV reference point, rebuilding goals must be restrained to the objectives associated with the lower-abundance stable state, \( N^L_{\text{msy}} \) being the obvious target. The key to this assessment is the value of the type-III reference point and particularly whether that value falls below zero.

Options for rebuilding

Most oyster revitalization programs have rebuilding goals and most are premised on recruitment enhancement (e.g., Haven and Whitcomb, 1983; Abbe, 1988; Leffler, 2002). This is typically accomplished through judicious shell planting, that also improves habitat integrity (Powell et al., 2006; Powell and Klinck, 2007). Both restora-
tion goals and methods have received considerable attention (e.g., Breitburg et al., 2000; Mann, 2000).

Restoration goals are dramatically impacted by the location of type-II reference points in relation to stock abundance. Type II is the goal under MSY management objectives, and by the presence of type IV and the differential between types II and III. The difference between type II and type III affects 1) the ease of transition from one stable point to another and 2) the impact on fishery yield during the transition. As the differential increases, from the example in the surplus production trajectory of Figure 6 to that in Figure 7 for instance, the limitation on fishery yield during the transition must increase. The obvious incongruity will be an observed increase in abundance of marketable stock during times of decreased allocation necessitated by the transitory limitation on surplus production coincident with the type-III reference point. This apparent inequity will likely exacerbate the natural adversarial relationship that exists between regulator and industry. The frequently complex relationship between economics and biology in fisheries management is well known (Lipton and Strand, 1992; Mackinson et al., 1997; Imeson et al., 2002). Thus several questions come to the fore. Can rebuilding to \( N_{\text{msy}} \) be accomplished? This depends on the existence of type IV. Does one try to rebuild to \( N_{\text{msy}} \)? This depends on the willingness of the fishery and management to forgo catch yields during times of increasingly high abundance, possibly for an extended period, so that the population shifts to the higher regime.

Regime shifts of long-term stability almost certainly come with a type-IV reference point. In this case, even the closure of the fishery will not generate enough surplus production to rebuild past the type-III low. Recognizing the existence of such a barrier is critical. Presumably, a massive recruitment enhancement program could be implemented to artificially affect a regime shift. Patience may be the better alternative, using the \( N_{\text{msy}} \) value of the present regime as the management goal.
while awaiting the rare sequence of events generating a natural transition to the alternate stable state.

Harvest goals

Included in Figures 4–7 is an estimated allowable catch as a fraction of the stock. The values of surplus production given in Figures 4–7 are expressed in numbers, perforce as they are the data source from which the underlying biological relationships are derived. The estimate is provided with some trepidation because the present model does not take into account the differential in growth across the salinity gradient and therefore tends to overestimate the number of animals of market size in the population as a whole. Moreover, the model assumes absolute constancy in the relationship of brood size in the population as a whole. Moreover, the model may overestimate the fraction of the stock available for harvest in any given year. The formulation of Klinck et al. (2001) is a preferred option to obtain fishery allocations. Finally, the model consistently predicts a higher harvestable fraction at low abundance than at high abundance. An abettor in this trend may be the reliance of setting larvae more and more on the shell resource at low abundance than on the standing crop of living individuals. However, some portion of this outcome is likely due to an inability to accurately extrapolate the primary biological relationships below $0.8 \times 10^9$ animals. Such low abundances have not been observed and therefore the extrapolation is likely to be increasingly in error at lower and lower abundances. We do not give complete credence, therefore, to the proportional increase in harvestable fraction at low abundance indicated by the surplus production trajectories depicted in Figures 4–7.

From Figure 3 we observe that the range of abundances assigned to the various reference points varies little among simulations describing a range of assumptions about natural mortality and recruitment rate. By contrast, the range of surplus production is prodigious. Thus, an abundance goal distinguishing the standing crop of living individuals. However, some portion of this outcome is likely due to an inability to accurately extrapolate the primary biological relationships below $0.8 \times 10^9$ animals. Such low abundances have not been observed and therefore the extrapolation is likely to be increasingly in error at lower and lower abundances. We do not give complete credence, therefore, to the proportional increase in harvestable fraction at low abundance indicated by the surplus production trajectories depicted in Figures 4–7.

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Conclusions

The oyster population in Delaware Bay exhibits a population dynamics that is not normally described in commercial species. One reason is the presence of distinct and dynamically stable multiple stable points delimited by temporally rapid regime shifts. The result of this complexity is a series of reference points identified by the trajectory of surplus production, which departs dramatically from the simple Schaeffer curve (e.g., Zabel et al., 2003). We define four reference point types in terms of surplus production, its derivative, and the rate of change of this derivative (Table 2). In Delaware Bay, the surplus production trajectory likely manifests two stable points and the carrying capacities associated with them and these agree relatively well with the observed stable points.


3 Gulf of Mexico conditions with rapid growth (Ingle and Dawson, 1952; Butler, 1953; Hayes and Menzel, 1981) and multiple spawns per year (Hopkins, 1954; Hayes and Menzel, 1981; Choi et al., 1993, 1994) are examples of C. virginica under more r-selected conditions.
states in the population time series (Fig. 9). For each of these type-I reference points, a maximum in surplus production also exists. The presence of two stable states assures a type-III reference point that is a measure of the ease of transition between the two stable states and provides information on the likelihood that management can artificially impose a transition. In Delaware Bay, the type-III surplus production value may be negative. In this case, a type-IV reference point exists, a point-of-no-return. If the type-III reference point is positive, a quasi-stable state exists at low abundance that can be stabilized by overfishing. The existence of a positive type-III reference point imposes a particular conundrum to management in that rebuilding requires a reduction in fishery yield as abundance increases over a substantive abundance range.

The simulations show the uncertainty imposed by the limitations on accurate knowledge of the biological relationships. One noteworthy observation is that the location of the reference points undefined by a specific surplus production value (e.g., \( S_t = 0 \)), namely types II and III, are relatively stable in position with respect to population abundance over a wide range of uncertainties in recruitment and mortality rates (Table 2). The surplus production values associated with these reference points are much more uncertain (Table 2). Thus, location is much better known than scale. As recommended by Beverton et al. (1984), different models are likely to be needed for short-term catch forecasts and estimation of abundance goals.

We describe reference points in the context of multiple stable states. The simplicity of the \( B_{\text{msy}} - K \) couple so emphasized in fisheries management fails when multiple stable states exist. That they may often exist is now well considered, although not yet inculcated into the oracle of fisheries management. Multiple stable points assure 1) that a type-III reference point exists, 2) that this point will impede the attainment of imprudently formulated rebuilding goals, 3) that a type-IV point-of-no-return may exist that establishes a barrier to rebuilding, as well as imposing the conditions at high abundance necessary for stock collapse, and 4) that a carrying capacity may exist at abundances well below historically high abundances and well below the simplistic promulgation of \( B_{\text{msy}} \) as half the carrying capacity established by the higher stable state. Use of the latter may impose impossible requirements for rebuilding a stock because the promulgated goal exceeds the carrying capacity for the controlling regime.

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